

**CLAIMS**

Having thus described our invention, what we claim as new and desire to secure by Letters Patent is as follows:

- 1        1. A method for making prioritized recommendations to a customer in the  
2        process of filling a market basket for purchase on an Internet commerce site,  
3        the method comprising the steps of:  
4                generating a matrix of training data;  
5                considering preferences based on associative and renewal buying  
6        history from the training data; and  
7                making a prioritized recommendation of items so as to maximize the  
8        likelihood that the customer will add to the market basket those items with  
9        higher priorities.
- 1        2. The method of claim 1, wherein the two preferences are estimated  
2        separately from the training data and combined in proper proportions to obtain  
3        an overall preference for item not yet in the market basket.
- 1        3. A method for making prioritized recommendations to a customer in the  
2        process of filling a market basket for purchase on an Internet commerce site,  
3        the method comprising the steps of:  
4                collecting statistics from training data;  
5                precomputing model parameters from the collected statistics; and  
6                recommending ordering for a given partial market basket based on the  
7        precomputed model parameters.
- 1        4. The method of claim 3, wherein the step of collecting statistics comprises  
2        the steps of:

- 3 (a) for each item  $j$ , obtaining  $n_j$  a number of baskets with item  $j$  purchased;  
 4 (b) for each item  $j$ , obtaining  $n'_j$  a number of baskets with  $j$  being a sole  
 5 item purchased;  
 6 (c) for each pair of items  $i$  and  $j$ , obtaining a number of market baskets  $n_{ji}$   
 7 with items  $j$  and  $i$  purchased together; and  
 8 (d) for each pair of items  $i$  and  $j$ , obtaining a number of market baskets  
 9  $n'_{ji}$  with items  $i$  and  $j$  being the only two items purchased.

- 1 5. The method of claim 4, wherein the step of precomputing model parameters  
 2 comprises the steps of:

3 (a) computing  $\mathbf{P}(\text{renewal}) = \frac{\sum_k n'_k}{\sum_k n_k}$  ;

4 (b) for each item  $j$ , computing  $\mathbf{P}(j) = \frac{n_j}{\sum_k n_k}$  ;

5 (c) for each item  $j$ ,  
 6 computing  $\mathbf{P}(\text{renewal} | j) = \frac{n'_j}{n_j} + \mathbf{P}(\text{renewal}) \left( 1 - \frac{n'_j}{n_j} \right)$  ;

7 (d) for each item  $j$ , computing  
 8  $\mathbf{P}'(j | \text{renewal}) = \mathbf{P}(\text{renewal} | j) \times \frac{\mathbf{P}(j)}{\mathbf{P}(\text{renewal})}$  ;

9 (e) for each pair of items  $i$  and  $j$  with  $n_{ij} \neq 0$ , computing

$$10 \quad \mathbf{P}(j \mid i) = \frac{n_{ji}}{\sum_k n_{ki}} ;$$

11 (f) for each pair of items  $i$  and  $j$  with  $n_{ij} \neq 0$ , computing

$$12 \quad \mathbf{P}(\text{renewal} \mid j, i) = \frac{n'_{ji}}{n_{ji}} + \mathbf{P}(\text{renewal}) \left( 1 - \frac{n'_{ji}}{n_{ji}} \right) ; \text{ and}$$

13 (g) for each pair of items  $i$  and  $j$  with  $n_{ij} \neq 0$ , computing

$$14 \quad \mathbf{P}'(j \mid \text{asso}, i) = \mathbf{P}(j \mid i) \times \frac{(1 - \mathbf{P}(\text{renewal} \mid j, i))}{(1 - \mathbf{P}(\text{renewal} \mid i))} .$$

1 6. The method of claim 5, wherein given a partial basket  $\mathbf{B} = \{i_1, i_2, \dots, i_k\}$   
 2 and  $\bar{\mathbf{B}}$  is a complementary set of items not in  $\mathbf{B}$ , the step of recommending  
 3 ordering for a given partial market basket comprises the steps of:

4 (a) if  $\mathbf{B}$  is empty, sorting items in order of decreasing  $\mathbf{P}(j \mid \text{renewal})$  and  
 5 returning this as an item preference ordering;

6 (b) if  $\mathbf{B}$  is non-empty, then

7 (i) computing  $\mathbf{P}(\text{renewal} \mid \mathbf{B}) = \min_{i_k \in \mathbf{B}} \mathbf{P}(\text{renewal} \mid i_k) ;$

8 (ii) compute a normalization factor  $\sum_{k \in \bar{\mathbf{B}}} \mathbf{P}'(k \mid \text{renewal}) ;$

9 (iii) for each item  $j \in \bar{\mathbf{B}}$ , computing

$$10 \quad \mathbf{P}(j \mid \text{renewal}) = \frac{\mathbf{P}'(j \mid \text{renewal})}{\sum_{k \in \bar{\mathbf{B}}} \mathbf{P}'(k \mid \text{renewal})} ;$$

- 11 (iv) computing a normalization factor  $\sum_{k \in \bar{\mathbf{B}}} \mathbf{P}'(j \mid \text{asso}, \mathbf{B})$  ;
- 12 (v) for each item  $j \in \bar{\mathbf{B}}$  , computing
- 13  $\mathbf{P}'(j \mid \text{asso}, \mathbf{B}) = \max_{i_k \in \mathbf{B}} \mathbf{P}(j \mid \text{asso}, i_k)$  ;
- 14 (vi) for each item  $j \in \bar{\mathbf{B}}$ , computing
- 15  $\mathbf{P}(j \mid \text{asso}, \mathbf{B}) = \frac{\mathbf{P}'(j \mid \text{asso}, \mathbf{B})}{\sum_{k \in \bar{\mathbf{B}}} \mathbf{P}'(k \mid \text{asso}, \mathbf{B})}$  ;
- 16 (vii) for each item  $j \in \bar{\mathbf{B}}$ , computing
- 17  $\mathbf{P}(j \mid \mathbf{B}) = \mathbf{P}(j \mid \text{asso}, \mathbf{B})\mathbf{P}(\text{asso} \mid \mathbf{B}) + \mathbf{P}(j \mid \text{renewal}, \mathbf{B})\mathbf{P}(\text{renewal} \mid \mathbf{B})$ ;
- 18 and
- 19 (viii) sorting items in order of decreasing  $\mathbf{P}(j \mid \mathbf{B})$  and returning this
- 20 as an item preference ordering.

1 7. The method of claim 6, wherein the step of sorting comprises the step of  
 2 using a final probability obtained for each item,  $\mathbf{P}(j \mid \mathbf{B})$ , of a customer buying  
 3 the item to maximize profit by recommendation.

1 8. The method of claim 7, wherein the step of using a final probability of an  
 2 item to maximize profit comprises the steps of:  
 3 assigning a profit amount,  $\$_j$ , to each item;  
 4 computing  $\mathbf{P}(j \mid \mathbf{B})\$_j$  for each item; and  
 5 ranking recommendations based on the computation of  $\mathbf{P}(j \mid \mathbf{B})\$_j$  for  
 6 each item.